

# Frequency comparison via optical fibers

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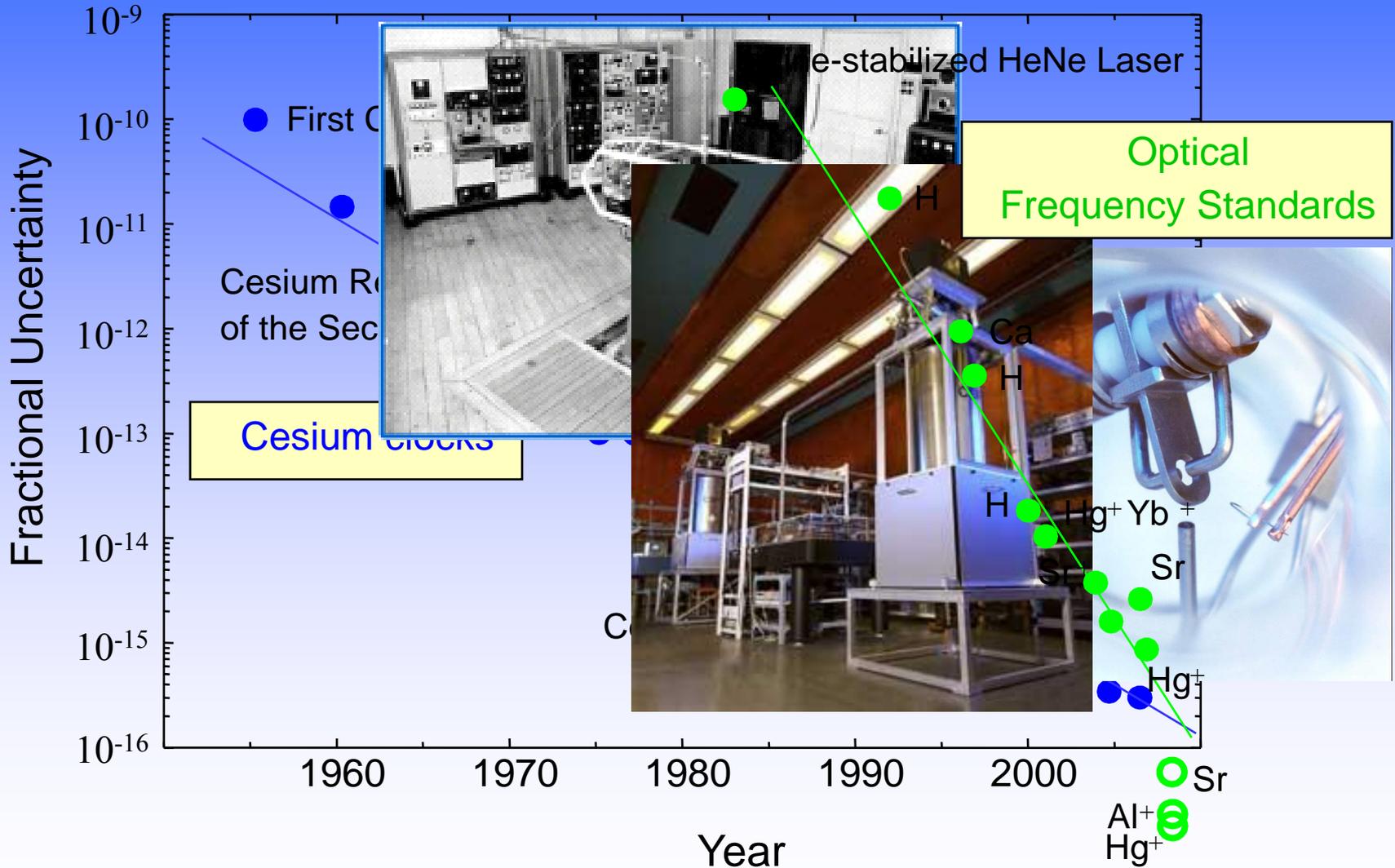
to user from user

Paris, May, 27. 2013



- Motivation
- Optical fiber links in a nutshell
- Frequency comparisons of optical clocks
- A future European network?
- Summary

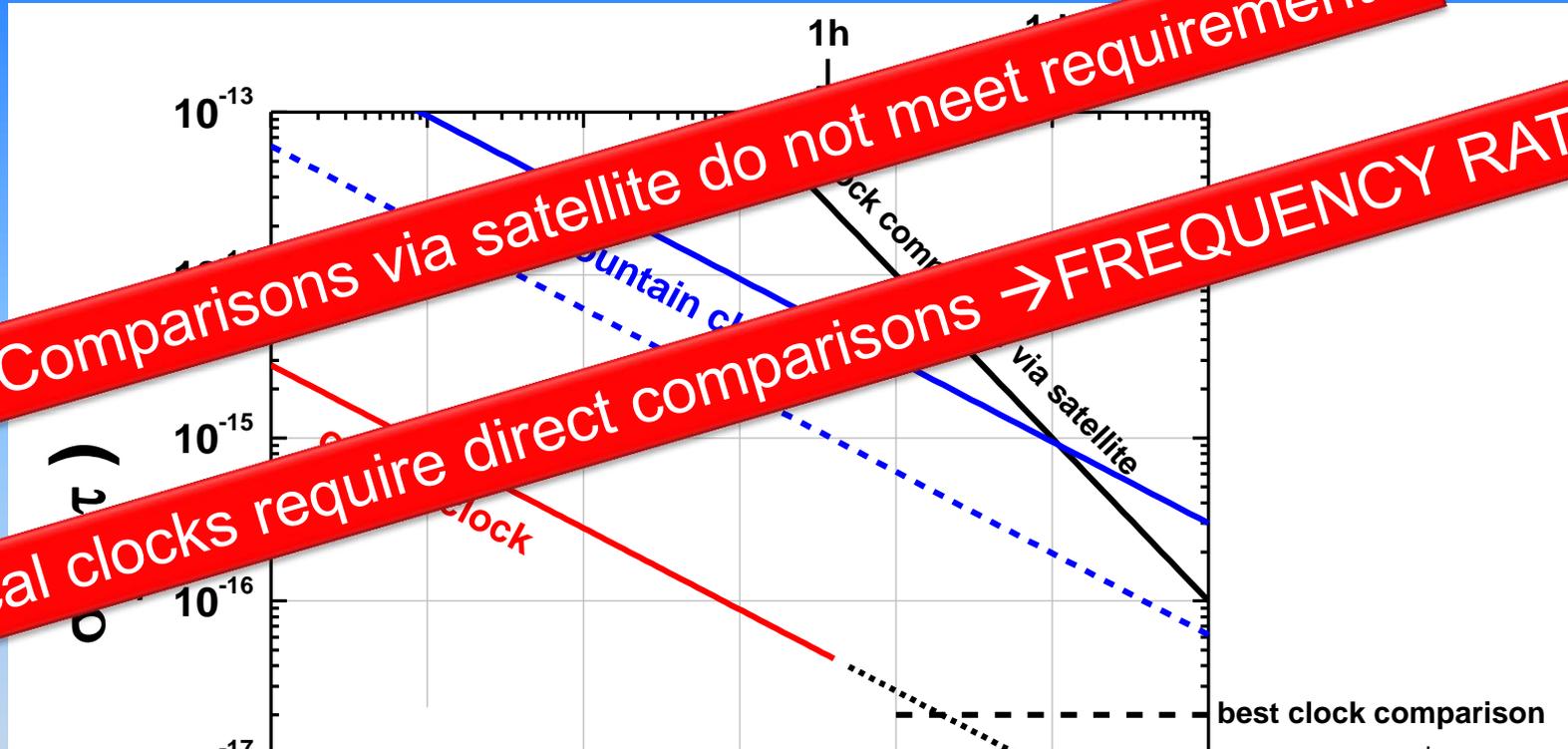
# Uncertainty of optical and Cs clocks



# Why use (better) clocks?

- **Clocks are ideal sensors to measure tiny effects with high precision.**
- **This mostly requires a frequency comparison between two clocks.**

# Clock comparison

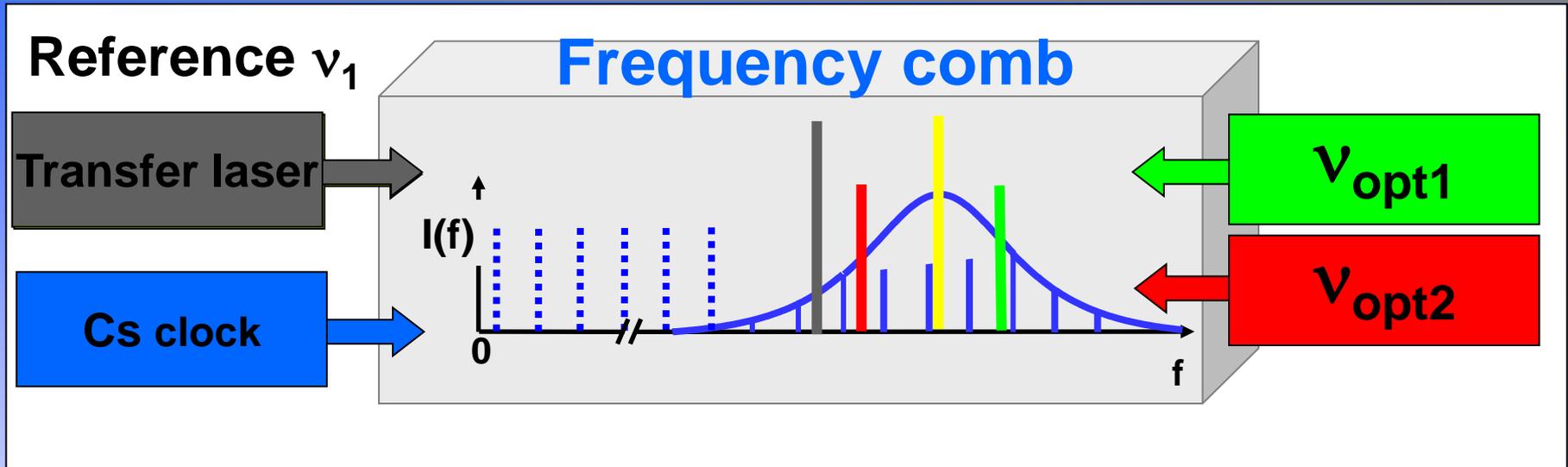


Comparisons via satellite do not meet requirements

Optical clocks require direct comparisons → FREQUENCY RATIO

How can we compare optical clocks over **large distance** without losing performance?

# Local comparison of frequency standards



$$\frac{\nu_{opt1}(A)}{\nu_{opt2}(A)} = \left( \frac{\nu_{opt1}}{\nu_1} \right)_A \cdot \left( \frac{\nu_1}{\nu_{opt2}} \right)_A$$

local comparison versus common reference  $\nu_1$

# TRANSFER of an OPTICAL CARRIER from location A to B

## Transfer A to B

local  
comparison at  
location A

Frequency standard

Frequency comb

Transfer laser  
 $\nu_1$

local  
comparison at  
location B

Frequency standard

Frequency comb

Transfer laser  
 $\nu_2$

fiber

$$\text{const} = \left( \frac{\nu_{opt1}}{\nu_1} \right)_A$$

$$\nu_1(A) / \nu_2(B)$$

$$\left( \frac{\nu_2}{\nu_{opt2}} \right)_B = \text{const}$$

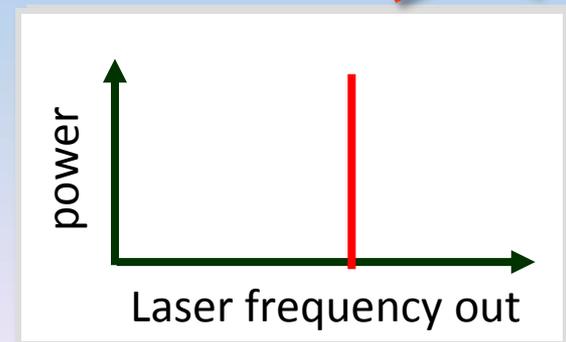
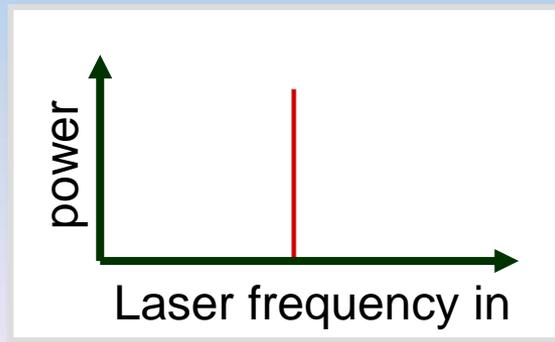
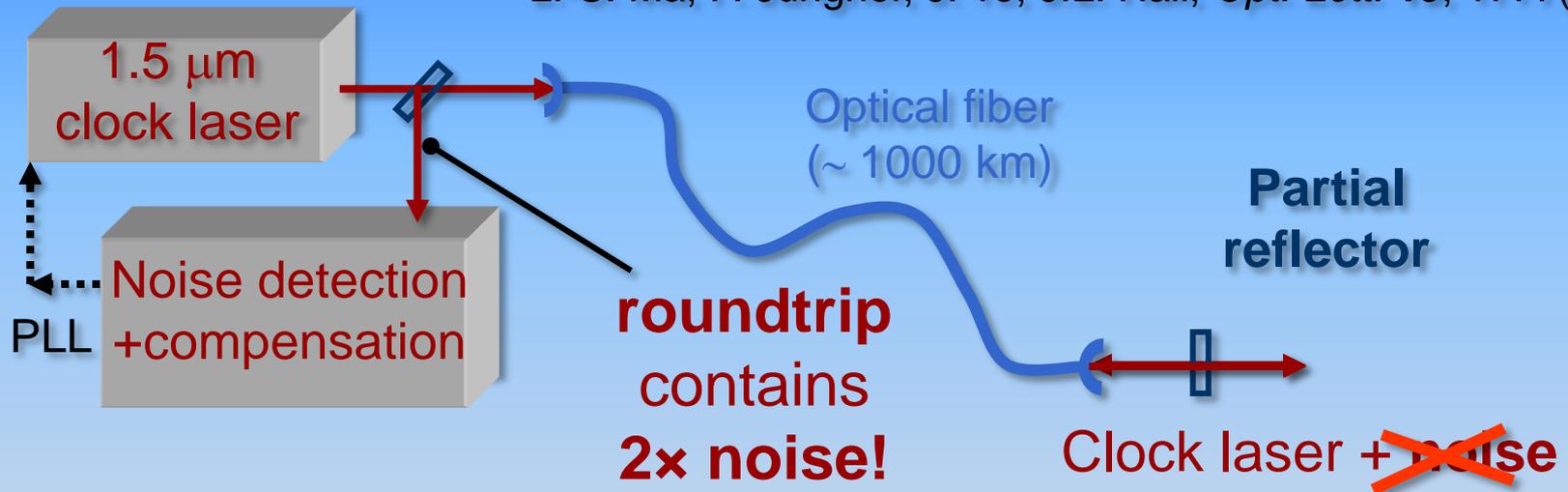


- Signal attenuation →
  - select low loss fiber: 0.2 dB/km
  - in-line bi-directional amplifiers: EDFA
- Stimulated Brillouin Scattering SBS →
  - keep input power below threshold: 5 mW
- Coherence of transmitted frequency →
  - use highly stable cw laser
- High isolation against environmental noise (thermal, acoustic, seismic, etc.) →
  - use fiber buried under ground
- Optical path length changes  $\Delta L$  →
  - compensate  $\Delta L$  by  $\Delta f$  using AO frequency shifter

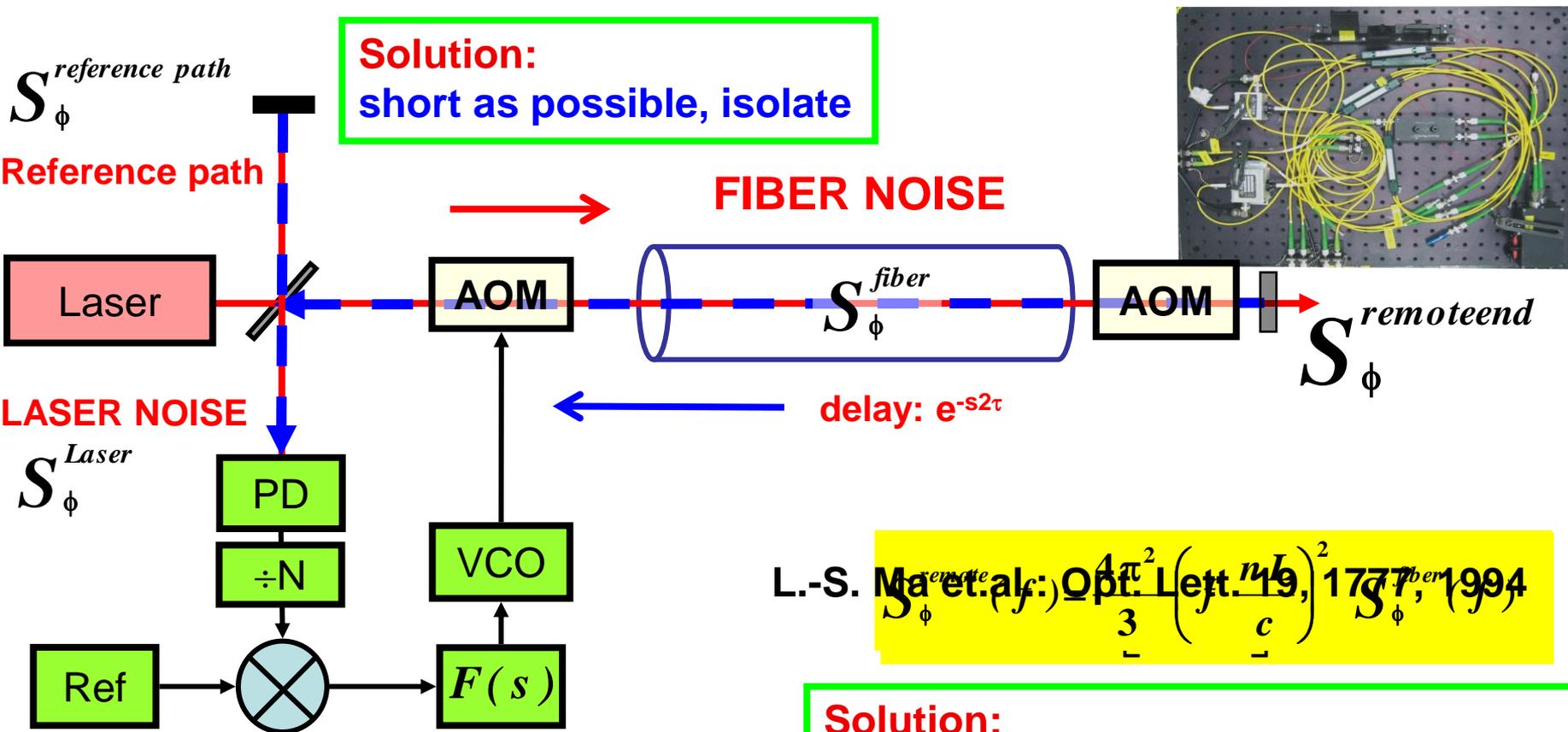
# Fiber Noise Cancelation

Compensation of frequency fluctuations due to length fluctuations\*:

\*L.-S. Ma, P. Jungner, J. Ye, J.L. Hall, *Opt. Lett.* **19**, 1777(1994)



# Fiber Noise Cancellation



L.-S. Ma et al.: Opt. Lett. 19, 1777, 1994

$$S_{\phi}^{remote} = \frac{4\pi^2}{3} \left( \frac{mL}{c} \right)^2 S_{\phi}^{fiber}$$

[1] Williams et al., JOSA B25,1284 (2008)

# Noise Cancellation Limit

Limited by:

1. Laser noise
2. Out of loop fiber
3. Delay unsuppressed fiber noise

$$S_{\Phi}^{remote}(f) = \frac{4\pi^2}{3} \cdot \left[ f \cdot \frac{nL}{c} \right]^2 \cdot S_{\Phi}^{fiber}(f)$$

P. A. Williams et al., *J Opt. Soc. Am. B* **25**, 1284 (2008)

Assuming:

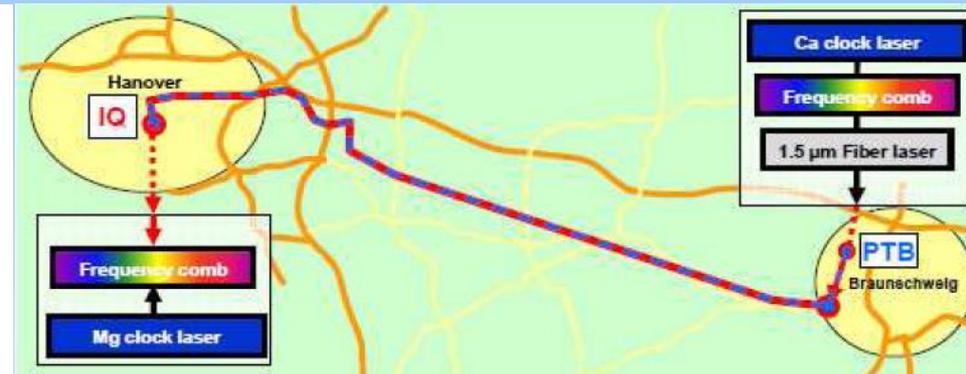
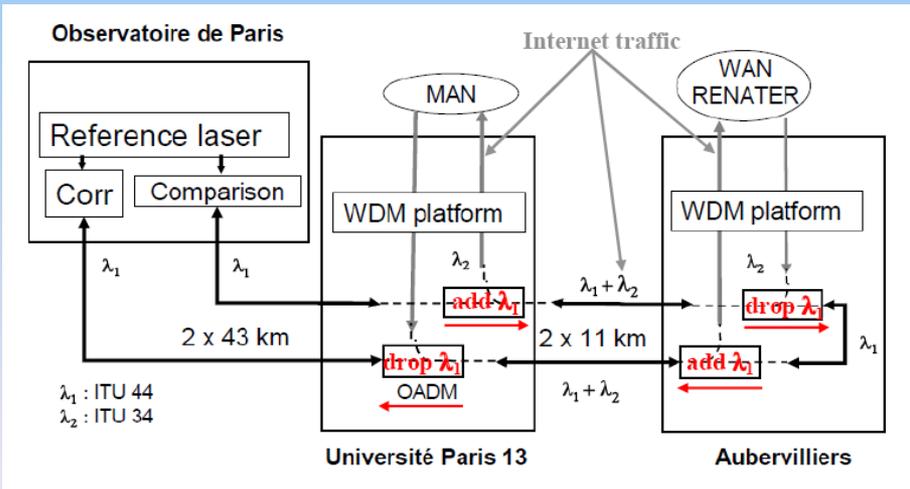
$$S_{\Phi}^{fiber}(f, L) \propto L \Rightarrow$$
$$S_{\Phi}^{remote}(f, L) \propto L^3$$

$$ADEV(D, \tau) \approx 2 \cdot 10^{-14} \times \sqrt{\left( \frac{D}{480 \text{ km}} \right)^3} \cdot \frac{1}{\tau}$$

# Frequency dissemination: two approaches

- Network with Data transmission
- **parallel to data traffic**
- requires:
- Access to the same “dark channel” in two fibers of the same bundle
- Bi-directional in-line amplifiers
- Additional channel for remote control

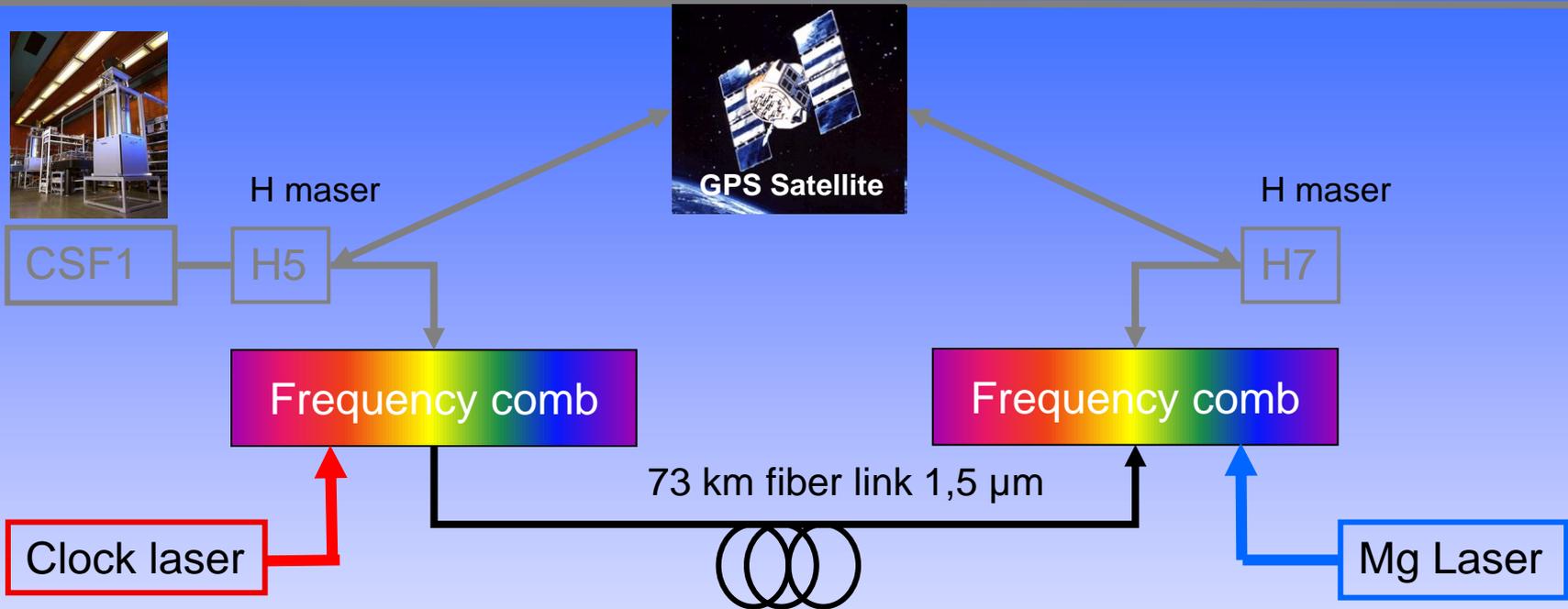
- “Dark Fiber”
- **Single user**
- requires :
- Access to the same “dark channel” in two fibers of the same bundle
- Bi-directional in-line amplifiers
- remote control (same fiber 1.3μm)



# Evaluation of a Mg frequency standard



# Clock laser comparison



Absolute frequency →

$$\frac{\nu_{Mg}}{\nu_{CSF1}} = \left( \frac{\nu_{Mg}}{\nu_{H7}} \cdot \frac{\nu_{H7}}{\nu_{NIR}} \right)_{IQO} \cdot \left( \frac{\nu_{NIR}^{IQO}}{\nu_{NIR}^{PTB}} \right) \cdot \left( \frac{\nu_{NIR}}{\nu_{H5}} \cdot \frac{\nu_{H5}}{\nu_{CSF1}} \right)_{PTB}$$

Stability →

$$\frac{\nu_{Mg}(t)}{\nu_{CL}(t)} = \left( \frac{\nu_{Mg}(t)}{\nu_{NIR}(t)} \right)_{IQO} \cdot \left( \frac{\nu_{NIR}^{IQO}(t)}{\nu_{NIR}^{PTB}(t)} \right) \cdot \left( \frac{\nu_{NIR}(t)}{\nu_{CL}(t)} \right)_{PTB}$$

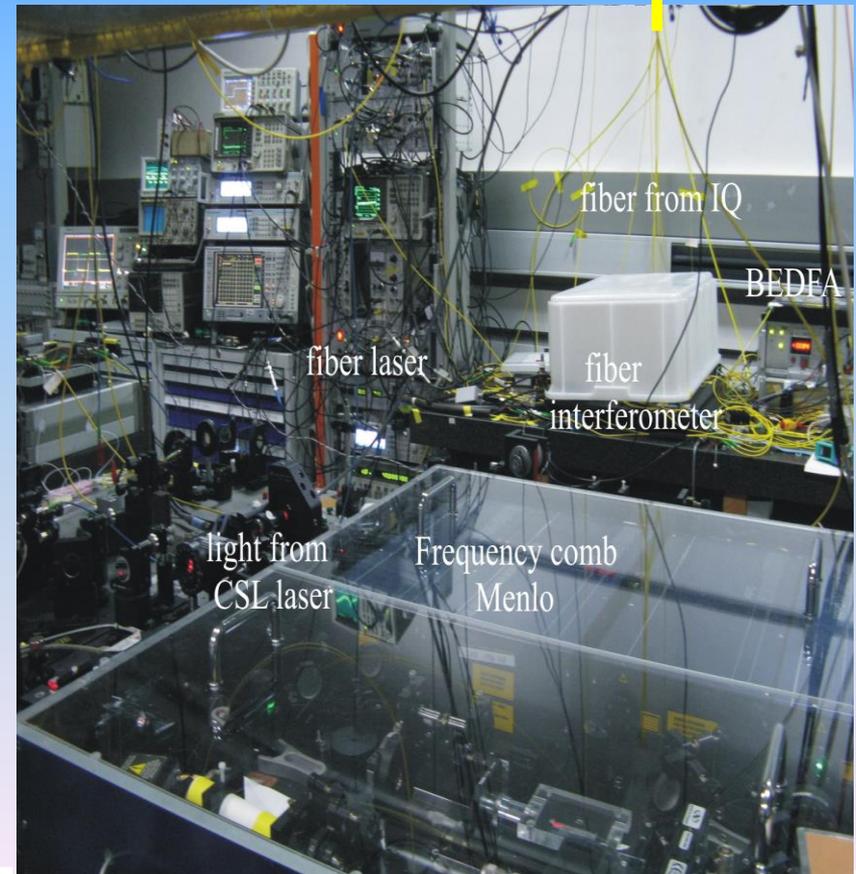
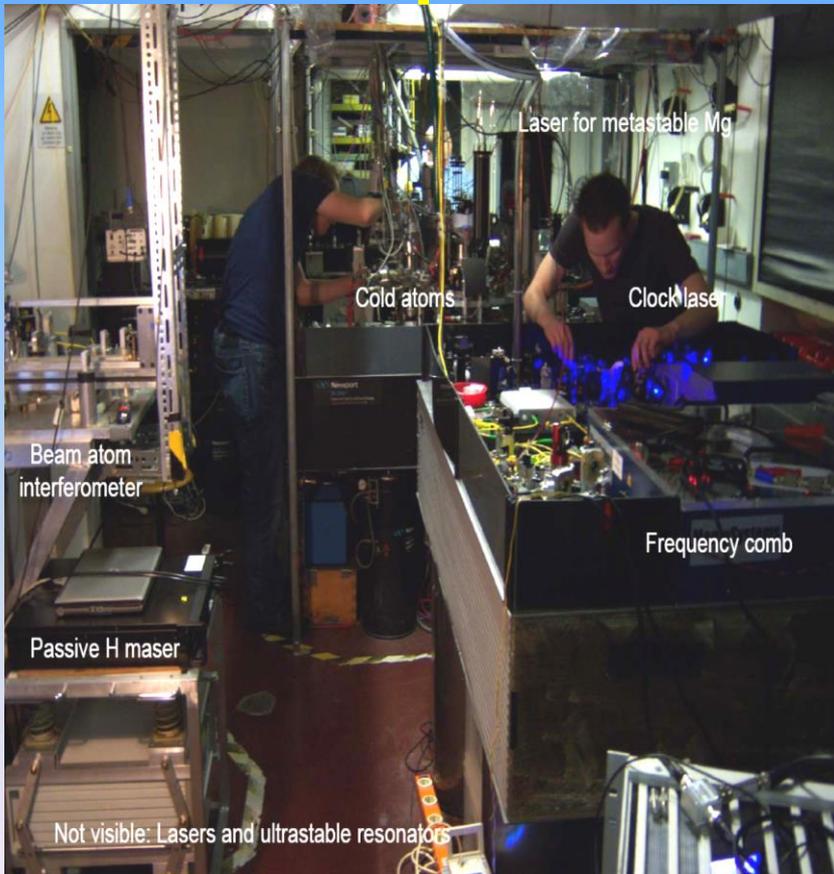
# Improving an optical clock laser

Mg-clock at IQ, LUH

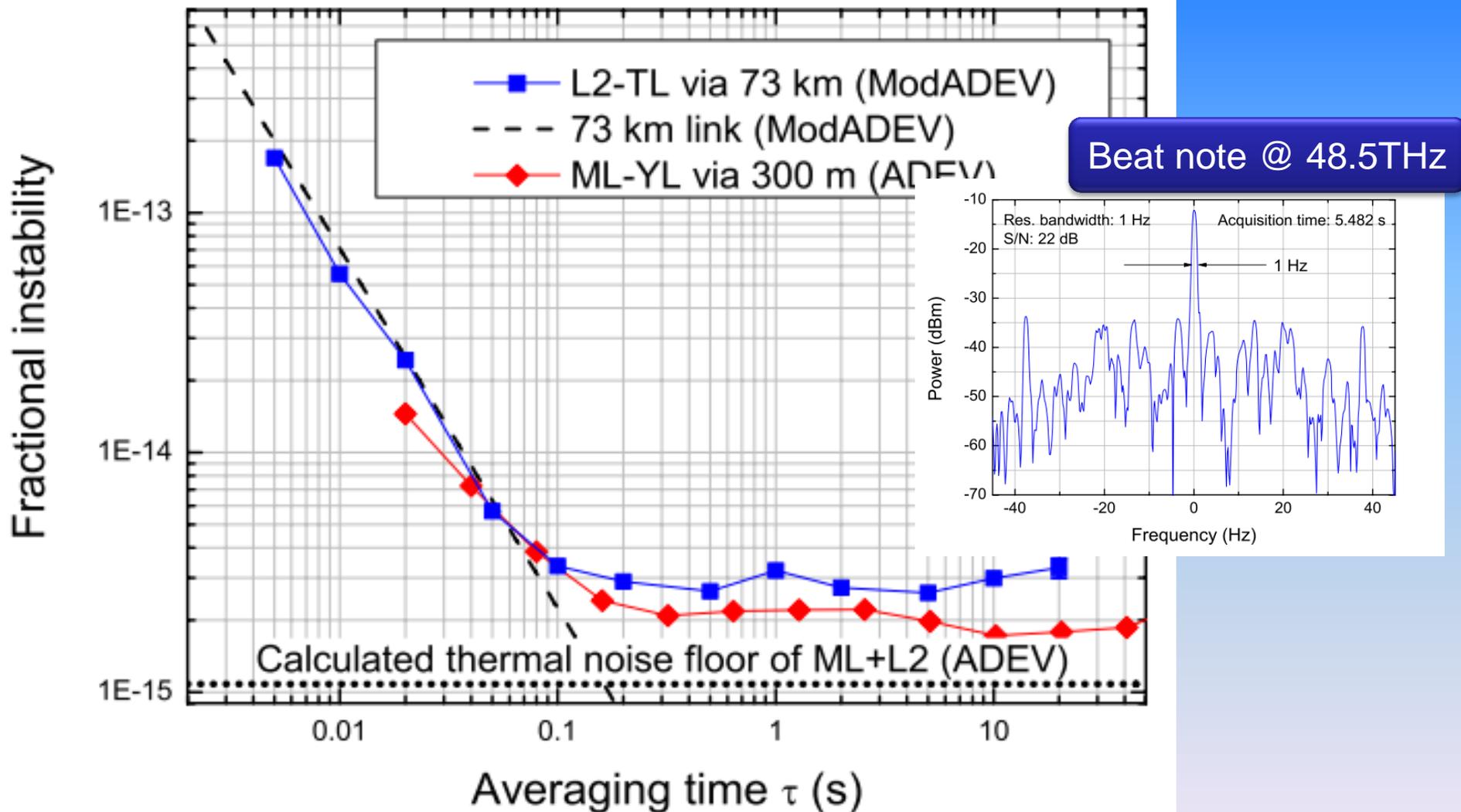
PTB, Braunschweig

74 km

Fiber from PTB

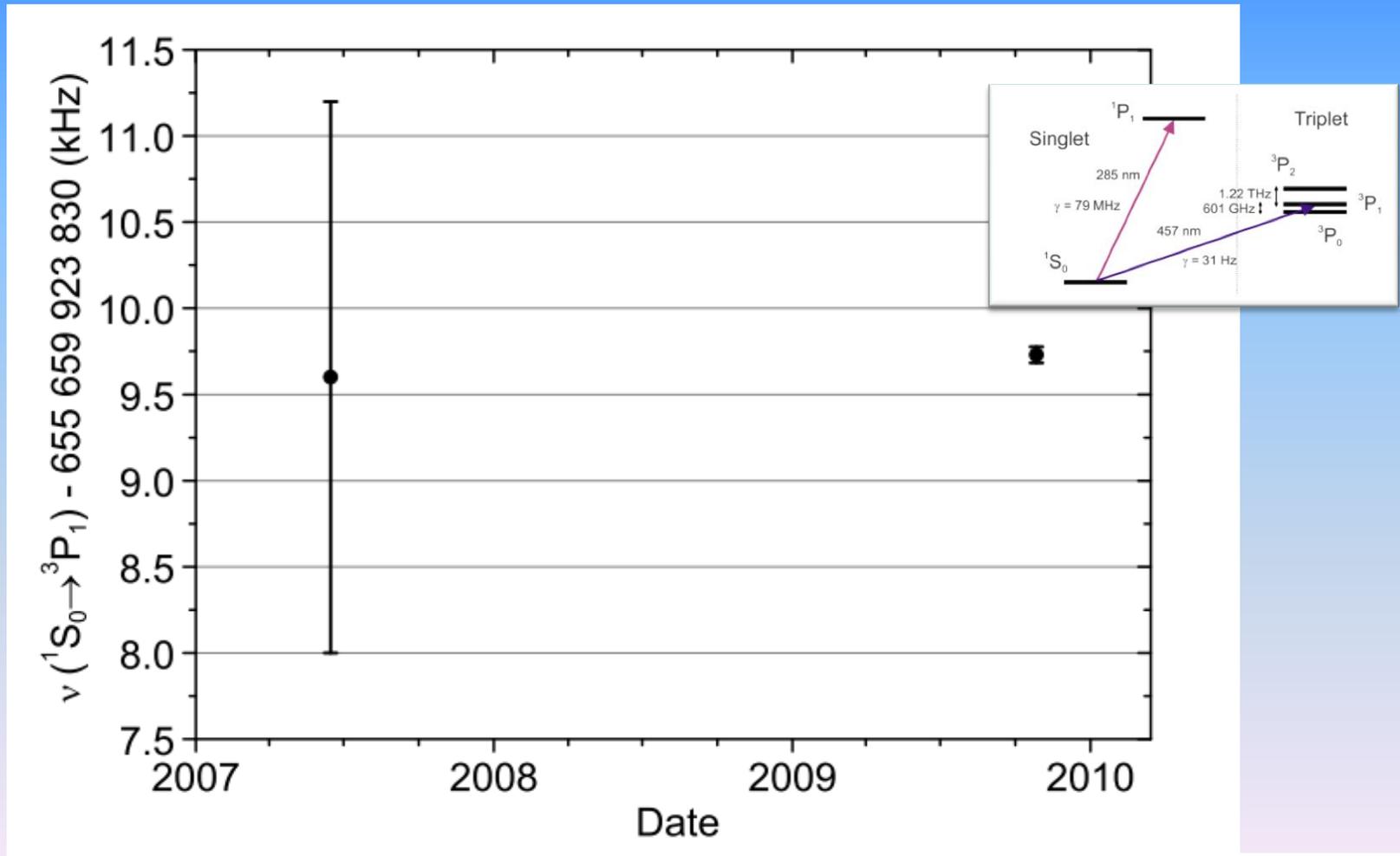


# Characterization of remote clock laser



# $^1S_0 \rightarrow ^3P_1$ clock transition of $^{24}\text{Mg}$ vs. remote CSF1

$$\nu(^{24}\text{Mg} : ^1S_0 \rightarrow ^3P_1) = 655\,659\,923\,839\,730\,(48)\text{ Hz.}$$



# Some details of the 920 km link

- 2 *dark* fibers ( ITU-T G.652)

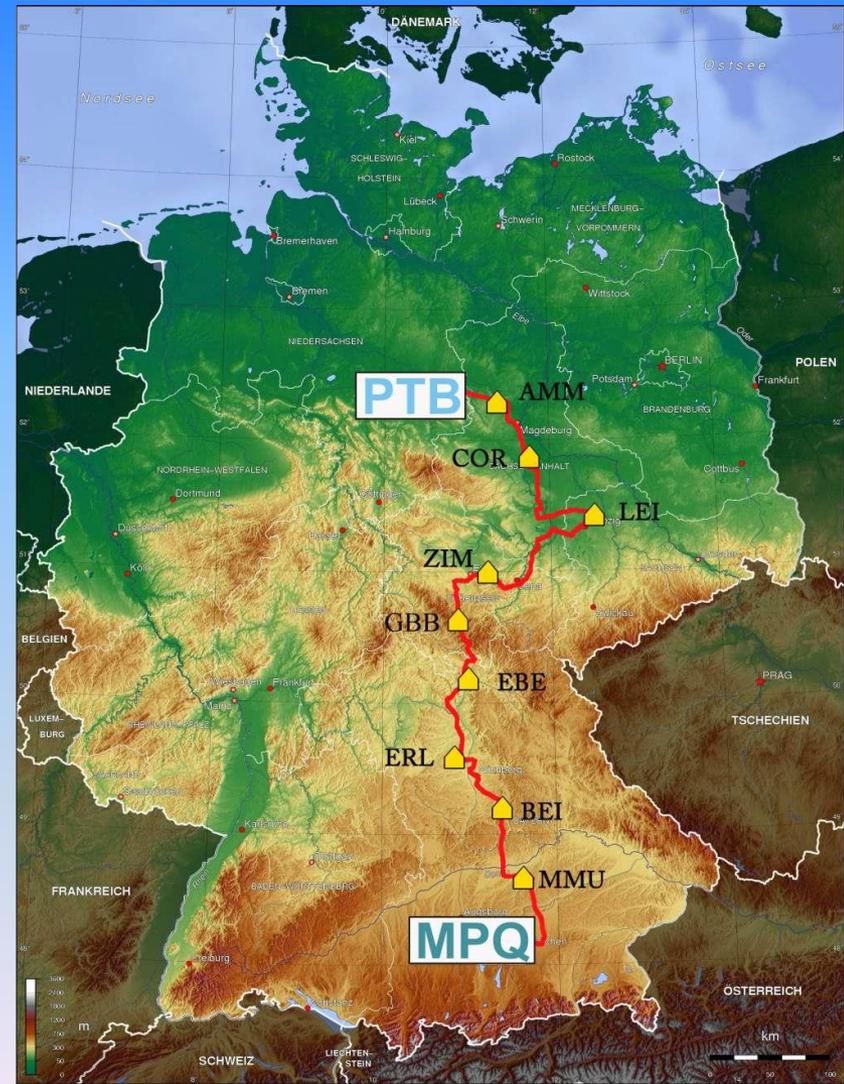
$n \sim 1.4681$  at 1550 nm

$A \sim 0.23$  dB/km

$CD \sim 18$  ps/(nmkm)

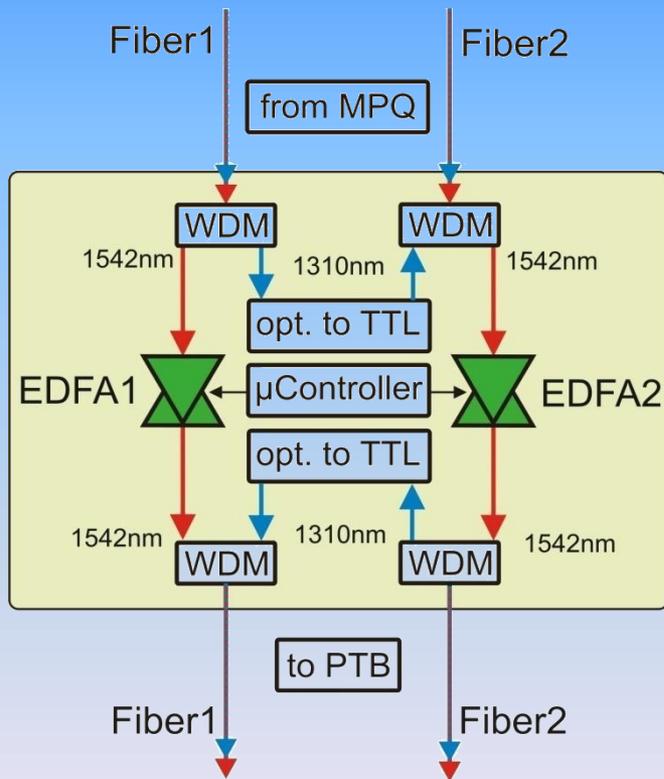


- Total fiber length 920 km
- Total one way loss >200 dB
- Access to the link at
  - 7 telecom containers
  - 2 computing centers



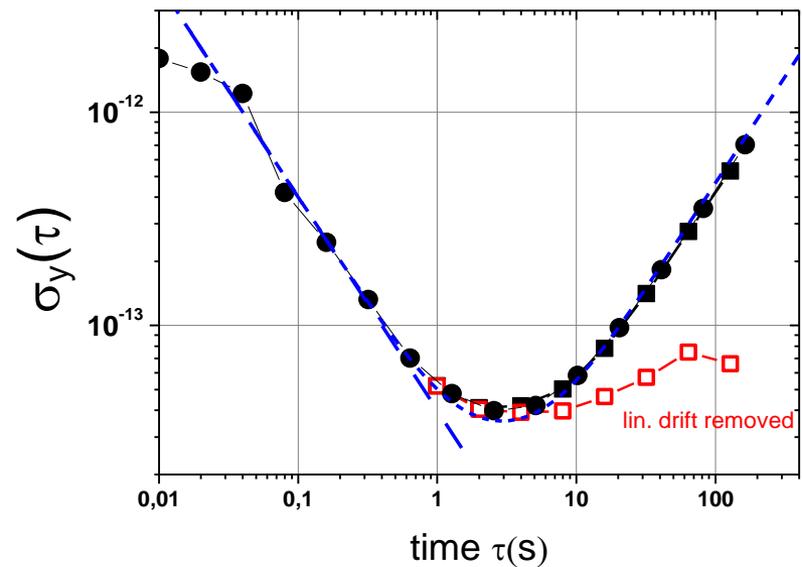
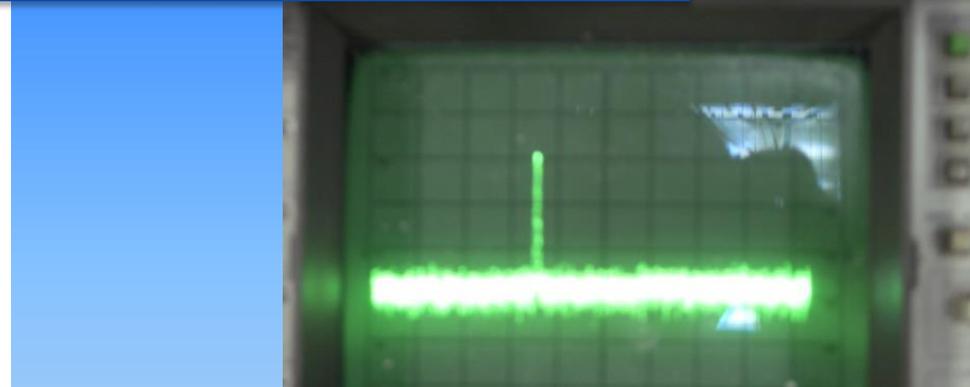
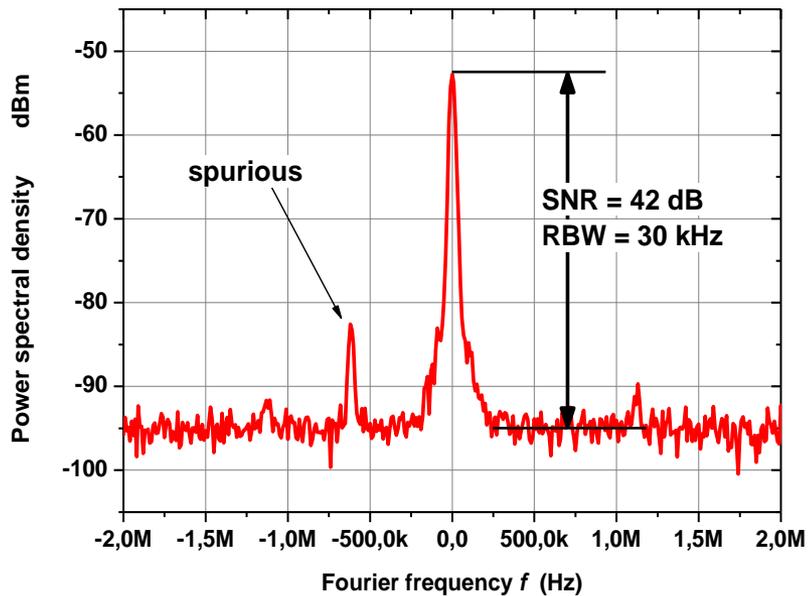
# Bi-directional amplifiers - EDFA

- Communicate with 16 bi-directional EDFAs along the fibre link via 1310 nm modulated signal

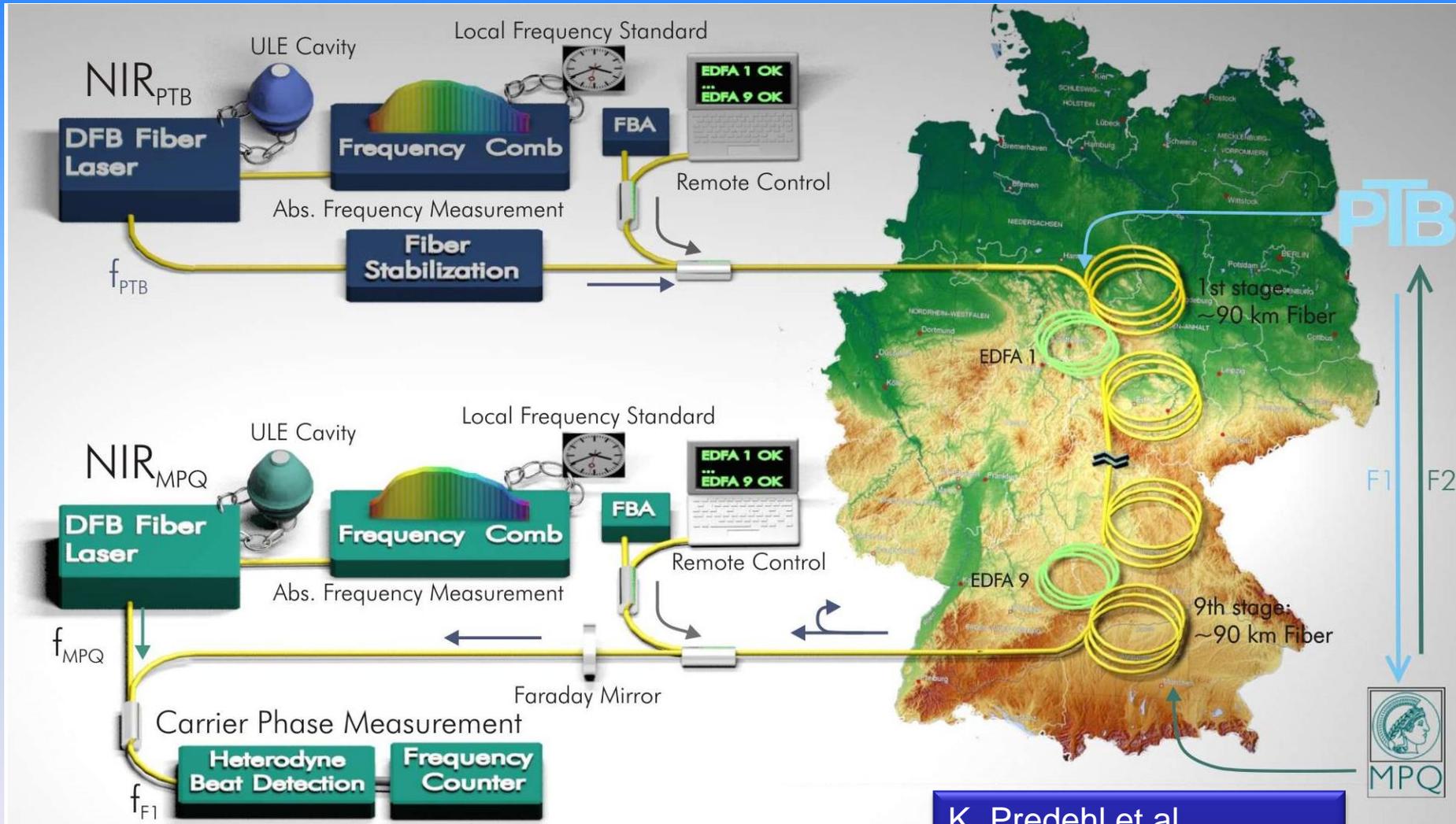


# Feb. 2010: first light through 900 km

## Beat note between $NIR_{PTB}$ and $NIR_{MPQ}$



# Experimental Setup

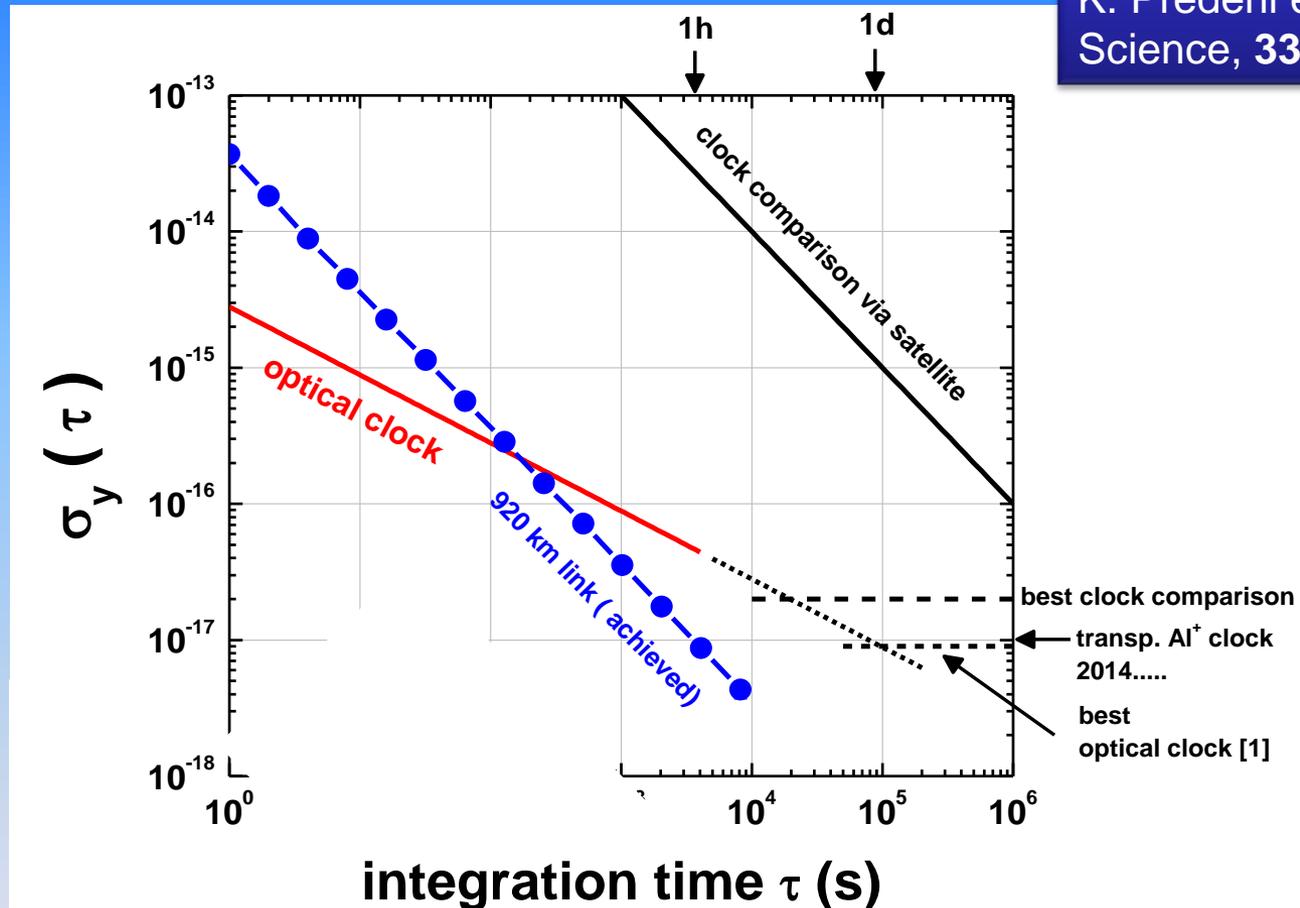


K. Predehl et al.,  
Science, 336, 441 (2012)



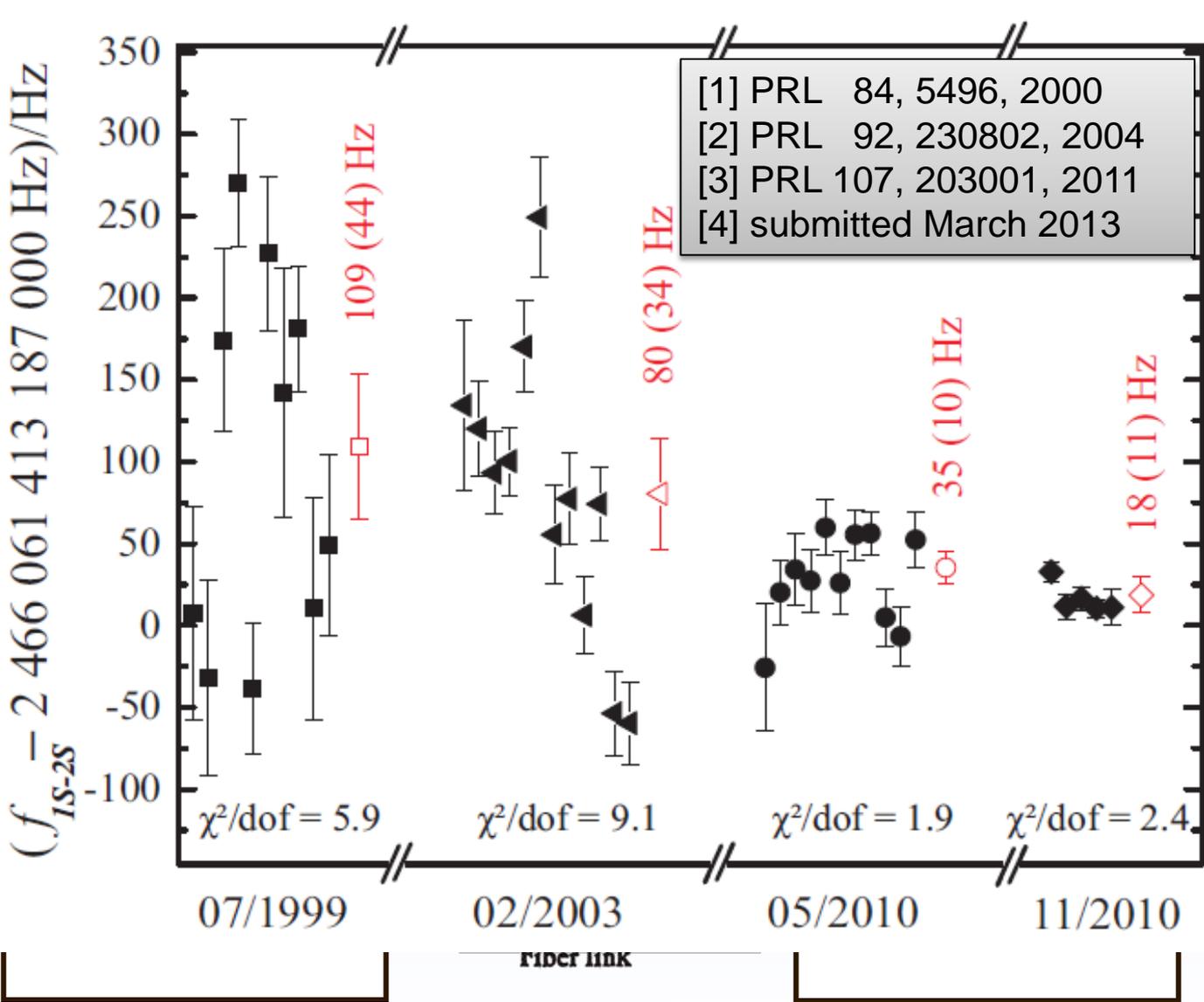
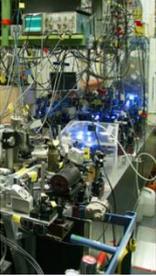
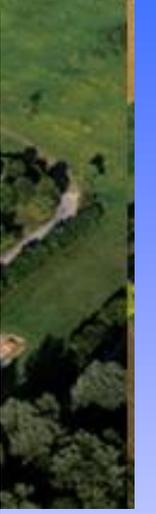
# Link Instability & Clock Comparisons

K. Predehl et al.,  
Science, 336, 441 (2012)



**Accuracy:  $(\nu_{\text{out}} - \nu_{\text{in}}) / \nu_{\text{in}} < 0.7 (3.7) \times 10^{-19}$  ( $< 100 \mu\text{Hz}$ )**

# 1S-2S Frequency measurement



- [1] PRL 84, 5496, 2000
- [2] PRL 92, 230802, 2004
- [3] PRL 107, 203001, 2011
- [4] submitted March 2013





Sebastian Raupach



EFTF student contest  
2010 2011



Stefan Droste



**Opt. frequency standards**

- Uwe Sterr
- Christian Lisdat
- Stefan Falke
- Thomas Legero

**Opt. cavities & stable Lasers**

- Thomas Legero
- Thomas Kessler
- Christian Hagemann



**Frequency measurement & dissemination**

- Burghard Lipphardt, Thomas Legero, Osama Terra, Sebastain Raupach, Gesine Grosche

MAX PLANCK INSTITUTE FOR THE SC

**Cs Clocks**

- Andreas B...
- Stefan Weyers



**MPQ Garching**

- Katharina Predehl
- Stefan Droste,
- T. W. Hänsch,
- Thomas Udem
- Ronald Holzwarth

# Giorgio's Dream around 2006 / 07



## JRP-Coordinator

PTB, Germany



## Funded JRP-Participants

BEV, Austria



INRiM, Italy



MIKES, Finland



NPL, United Kingdom



OBSPARIS, France



SP, Sweden



UFE, Czech Republic



VSL, The Netherlands



Dutch  
Metrology  
Institute

## Unfunded JRP-Participants

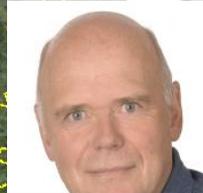
CESNET, Czech Republic



# NEAT-FT Participants



**NMIs participating in JRP**



All fiber links are operated in collaboration with NRENs



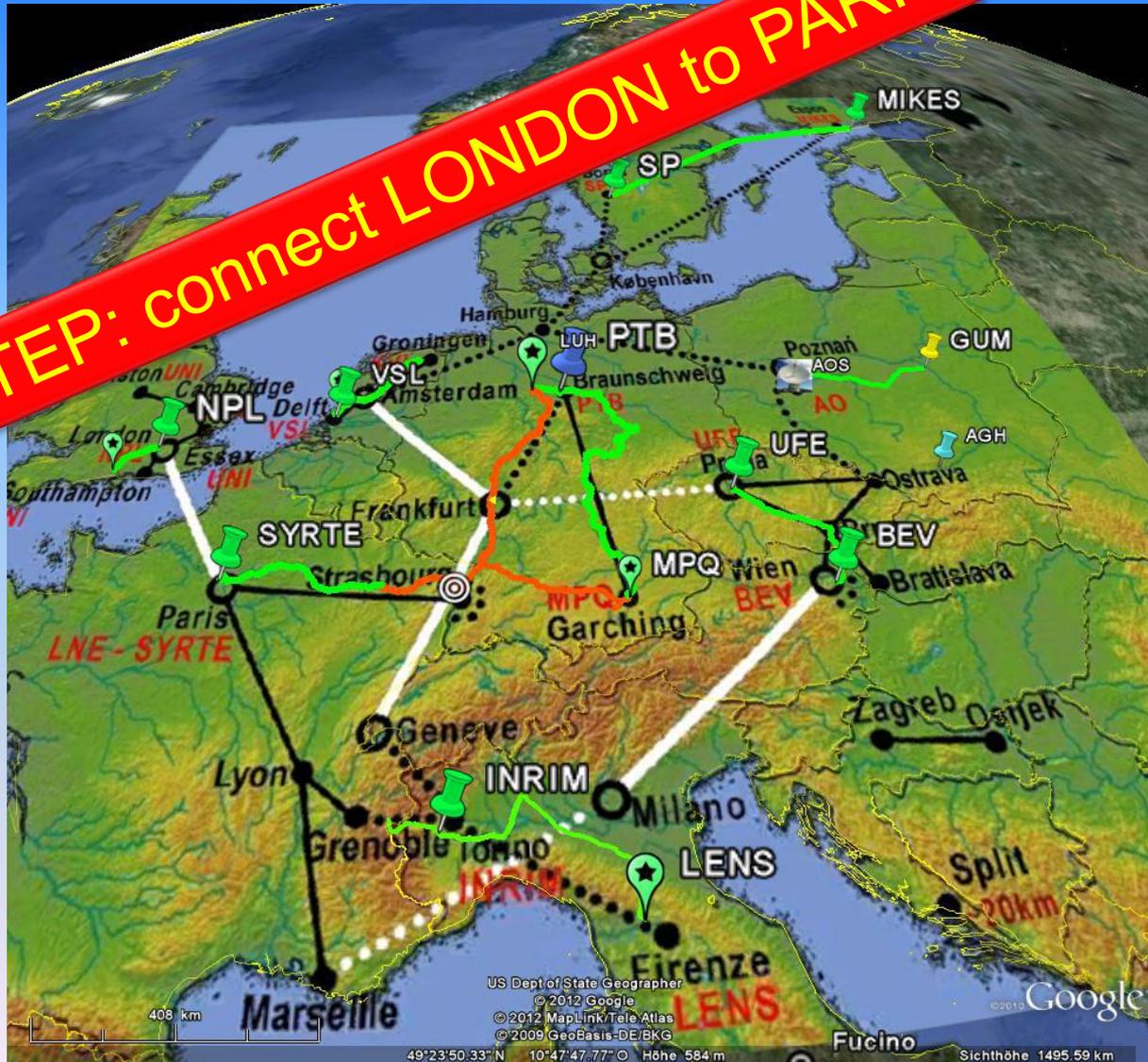
# Braunschweig - Paris Link via Frankfurt

Contract with GasLine Company has been signed last week!!!



# Fiber links in Europe via GEANT

**NEXT STEP: connect LONDON to PARIS**



# Comparisons between Cs clocks and recommended secondary representations

- Frequency ratio measurements at the  $10^{-17}$  level
  - Comparisons of remote optical clocks

✓ Independent systematics

✓ Test of fundamental physics

- Consistency checks

GÉANT NPL / SYRTE / PTB

PTB / QUEST

JRP ITOC 2013-16

recent work at PTB

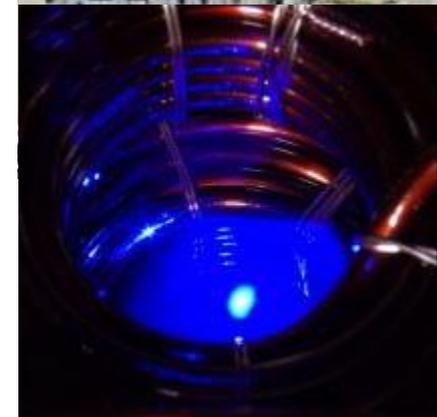
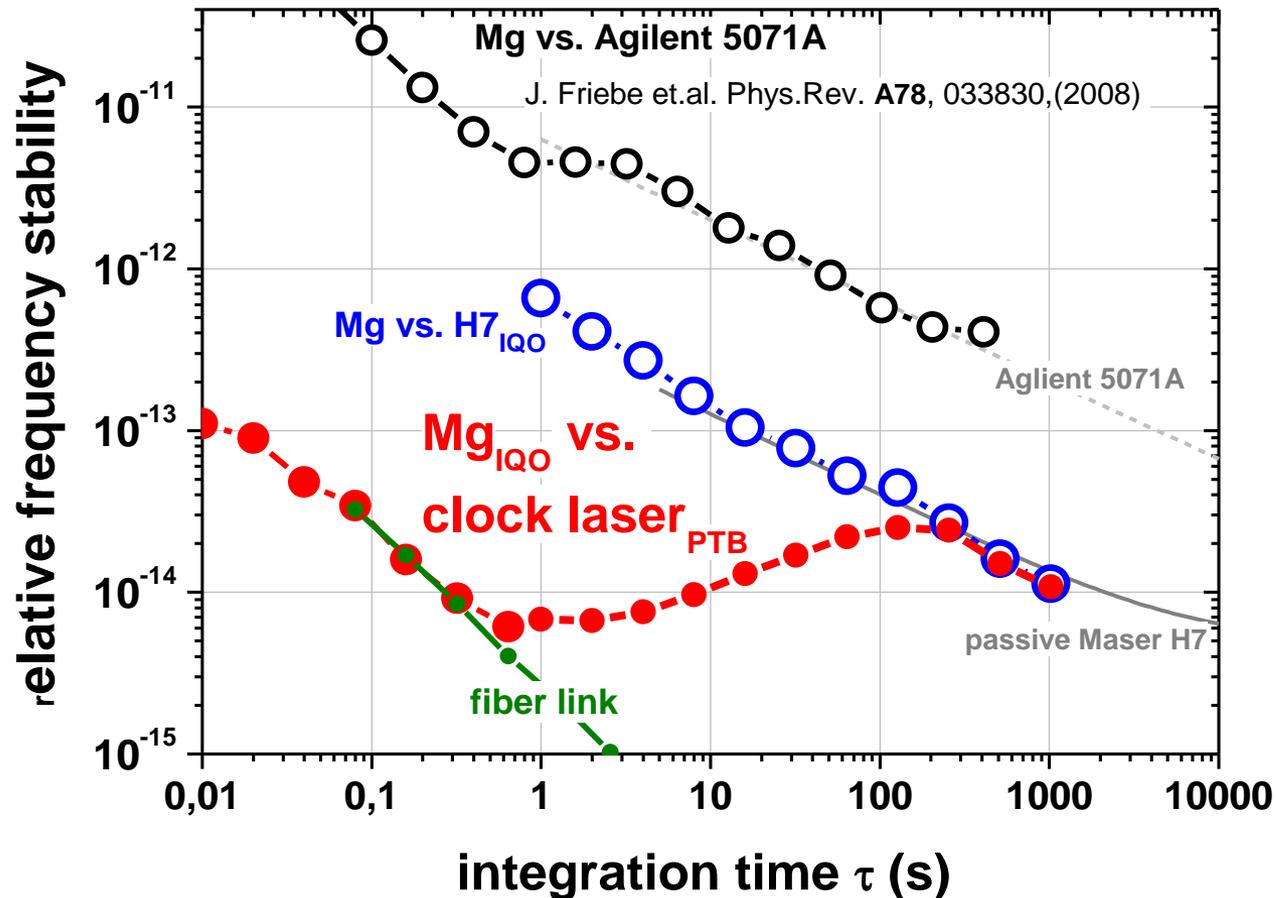
Cs	X								
Al <sup>+</sup>	X	X							
Hg <sup>+</sup>	X	X							
Sr <sup>+</sup>	X			X					
Yb <sup>+</sup> (E2)	X	○		★	X				
Yb <sup>+</sup> (E3)	X	○		★	★	★			
Yb	X								
Sr	X	○		○ ★	X	X	○	X	
Rb (MW)	X								X
Representation of SI: <b>s</b>	Cs	Al <sup>+</sup>	Hg <sup>+</sup>	Sr <sup>+</sup>	Yb <sup>+</sup> (E2)	Yb <sup>+</sup> (E3)	Yb	Sr	Rb (MW)

# Congratulations





# Result: Mg Frequency standard



# Installing Equipment

